# What is future of China's water needs?

Jiayue Qi Jianing Zhao Rucheng Du

February 4, 2013

# Contents

1	Sun	nmary	3
2	Intr	oduction	4
3	Res	tatement of the Problem	5
4	Fore	ecasting the Water Needs in 2025	5
	4.1	Grey Theory Background	5
	4.2	GM(1,1) Model	6
	4.3	Data Processing	7
	4.4	Data Analysis and Interpretation	8
5	Nor	nlinear Programming	14
	5.1	Original Model	15
	5.2	Shortest Path Problem Model	17
		5.2.1 The background	17
		5.2.2 <i>Dijkstra</i> algorithm	17
6	Opt	imization Model for Nonlinear Programming	21
	6.1	AHP Background	21
	6.2	Multi-objective Linear Weighting Function	21
	6.3	Optimal Model and Data Interpretation	22
7	Sim	ulation Model	25
8	Def	ects of Our Models	27

9 Conclusion	27
References	29
10 Position Paper for China Government	30

# 1 Summary

Aiming at the fresh water problem in China, our paper is organized in four models.

1. Grey Prediction Model

Grey prediction is one of the methods that are good at forecasting data holding exponential growing tendency. In our model, we forecast industrial water, ecological water utilization and basic daily water utilization in 2025 basing on the historical data from 1995 to 2011 for these data are close to population, which is an obvious exponential growing model.

2. Non-linear programming model

In this model, we apply graph theory to solve the problem of water transfer between cities. We attain our ideas via shortest path problem and we solve a problem of weighted shortest path. We set the weights for 31 provincial capitals from two side points–distance and height. With the help of Lingo, we resolve a non-linear programming model (after satisfying the cities' water demand, we have the lowest cost by our solution).

- 3. As the second model is quite idealized, we introduce some improvements to make it more specific. Firstly, this model concludes economics, environment and population factors; secondly, we change the objective function of our non-linear programming model by using Multi-objective linear weighting function method. Then, vividly, we get a feedback of corresponding relationship between fresh water resources and environment, economics, the yield of water, population and water quality.
- 4. Basing on the three models above, we find WEAP, a software describing and simulating water transferring. Via WEAP, we establish a simulation model to analysis annually of water strategy from 2013 to 2025 dynamically.

Generally, our results show water transmission and dispatching quantitatively and we overall considerate storage and movement of fresh water and economics, environmental factors in our model. Our results fit well with the South-to-north water transfer project and some other water strategies as well.

# 2 Introduction

As is known to all that fresh water is the limiting-constraint for development in much part of the world, people need fresh water for drinking. The total amount of water on the earth is 1.4 billion square kilometers. There is plenty of water on the earth while the fresh water only takes 2.53% of it among which the 68.7% is glacier and is hard to explore. Nowadays, there is only 0.26% of the total water amount on the earth. People have consumed 54% of the available fresh water over the world. Meanwhile, the problem concerning pollution of fresh water is not eliminated till now. Then it's obvious that fresh water problem is a widespread concern all over the world. As for China, the problem cannot be even slighter. China is a country with heavily shortened fresh water and the conflicts between provision and need can never be calmed down. According to the statistics data, there are 20 million people having heavy problem drinking water and over 400 cities in the situation of longing for fresh water. There can be droughts in either part of China. What's worse, the fresh water of most parts of China has been polluted more or less.

In 1972, UNHEC (United Nations Conference on the Human Environment) announced, "the next crisis after oil crisis is water". Then in 1977 The United Nations Conference of Water emphasized further that, "water will soon be a deep social crisis". As time goes by, the earth is suffering more and more by "water crisis", such as the loss of biodiversity and bad influence on people's health from water pollution. All in all, this is allowed of no delays to consider about the problem of fresh water in the world. In China the government has made some giant projects such as South-to-north water transfer project. Besides, China has made many reservoirs to balance the great difference in time in China, especially southern part of China.

People have done much work before about the corresponding questions. In allocation model for water right by Wang Xuefeng and his partners, they present a linear programming model discussing distribution problem of fresh water in China. Chen Kangning, Dong Zengchuan and Cui Zhiqing put forward an original idea to evaluate water system in their paper evaluation of vulnerability of regional water resources system based on the fractal theory. Yan Jun and his cooperators create their idea of the relationship between Water resources carrying capacity factor and the South-to-north water transfer project in the paper the influence of South-to North water transfer project on the water resources load capacity of the Yangtze River basin and the methods to optimize the allocation of water resources, which enlighten our road ahead.

In this paper we have two main theocratical models, the first one is based on grey prediction to forecast water needs in 2025 and the second is based on non-

linear programming algorithm. The results of grey prediction give us a whole view of China's future water needs and then based on the prediction, we build programming model to balance water resource distribution and water demand both of which present unbalanced geographically and seasonally. To check our original strategy coming from programming model, we build a regional simulation model to dynamically simulate changes and relationships of water supply and demand. In addition, considering the complexity and speciality of China, we look through information about both China's present water strategy and foreign countries' researches and experience. Based on these steps of analyzing and modeling, we get our final water strategy for 2013 to meet water needs in 2025 and submit one position paper recommending to governmental leadership.

### **3** Restatement of the Problem

As everyone knows, fresh water is a strong restriction towards development in most part of the world. How to present an effective, feasible efficient water strategy via producing a mathematical model to describe the very strategy in 2013 for China's water needs in 2025? Addressing storagemovement and conservation is vital to some degree while some economical, physical and environmental factors are better to be included.

## **4** Forecasting the Water Needs in 2025

### 4.1 Grey Theory Background

When considering many realistic problems whose internal structure, characteristics and parameters cannot be comprehended thoroughly, we can only find a solution to build models by rational assumptions and logic deductions instead of understanding the internal mechanism like white-box approach. This kind of system including unknown information inside is called Gray System.

*Grey prediction* refers to utilizing GM model to forecast the development regulation of systematic characteristics and as well the moment when anomalies occur. These applications indeed use *gray process* instead of *random process* and *gray variations* instead of *random variations* by applying GM(1,1) model in gray theory.

*Grey prediction* has been extensively applied in fields of industry, agriculture, business, environment, society and military, especially when forecasting trends

of development in the future through available data at present.

### 4.2 GM(1,1) Model

Assume original data series as

$$x^{(0)} = (x^{(0)}(1), x^{(0)}(2), \dots, x^{(0)}(n))$$
(1)

and the 1-AGO formation of  $x^{(0)}$  is defined as

$$x^{(1)} = (x^{(1)}(1), x^{(1)}(2), \dots, x^{(1)}(n))$$
(2)

where

$$x^{(1)}(k) = \sum_{i=1}^{k} x^{(0)}(i), k = 1, 2, \dots, n$$
(3)

The GM(1,1) model can be constructed as a grey differential equation as

$$x^{(0)}(k) + az^{(1)}(k) = b, k = 2, 3, \dots, n$$
 (4)

Corresponding white differential equation is

$$\frac{dx^{(1)}}{dt} + ax^{(1)}(t) = b$$
(5)

Using least square method, we can get the solution of differential equation as

$$x^{1}(k+1) = (x^{0}(1) - \frac{b}{a})e^{-ak} + \frac{b}{a}, k = 1, 2, \dots, n-1$$
(6)

in which the boundary condition is  $x^1(0) = x^0(1)$ .

The process of least square method is as follows:

The mean series is 
$$z^{(1)}(k) = 0.5x^{(1)}(k) + 0.5x^{(1)}(k-1), k = 2, 3, ..., n$$
, given

$$u = (a, b)^{T}, Y = (x^{0}(2), x^{0}(3), \dots, x^{0}(n))^{T}, B = \begin{bmatrix} -z^{1}(2) & 1 \\ -z^{1}(3) & 1 \\ \vdots & \vdots \\ -z^{1}(n) & 1 \end{bmatrix}$$
(7)

then  $\hat{u} = (a, b)^T = (B^T B)^{-1} B^T Y$ .

To check the accuracy of consequences of the GM(1,1) model, we calculate the *residual series*  $\varepsilon^{(0)}$  of  $x^{(0)}$  in order to get a better results than calculating  $\varepsilon^{(1)}$  of  $x^{(1)}$  which is generally used. Computing formula is defined as

$$\varepsilon^{(0)}(k) = \frac{x^{(0)}(k) - \hat{x}^{(0)}(k)}{x^{(0)}(k)}, k = 1, 2, \dots, n$$
(8)

#### 4.3 Data Processing

To forecast the future water needs for 2025, we should get the real water supply in the past few years. In fact, the statistic data include a wide range of categories like surface water, underground water, waste, usage in agriculture, industry, residential assumption, etc. Considering the water assumption of agriculture will be dependent on climate change, changes of policies from government (when residential assumption or industrial needs cannot be satisfied, the amount of agriculture water supply will be reduced in some areas of China, we ignore this kind of water usage for water dispatching in the next section. On the one hand, ignoring agricultural water assumption is consistent with real situation and policies of China, even though this category occupies a big part of water usage according to statistics (above 50%). On the other, except agricultural consumption, most of water usage, like residential and industrial consumption, are relevant with the growth of population. In addition, the waste of water supply is minimal, which in most provinces occupies less than 1%, thus the water supply is approximately equal to the water assumption. To exclude the agricultural water assumption, we use GM(1,1) model to forecast water needs in only urban area including production water supply and daily water needs of 31 provinces in China at first. Then we find that the accuracy of these fitting curves is sometimes not good enough as expected previously. Then we search more information about circumstances of these provinces and also the precise implications of statistics like what dose water supply means and includes. Finally, we decide to use water assumption excluding agricultural supply of both urban area and other area to calculate fitting curves again. Comparing the two consequences using different data gives us some new understandings and encouragingly, the second results come to a better fitting effect in most provinces. To be clear, for the second fitting processing results, we only use data ranging from 2002 to 2011 instead of that from 1997 to 2011 when calculating first fitting, because we later consider that China had natural disasters like flood in during 1990s which may influence the water needs increasing regulation relevant to population increase. Total curve pictures are attached in the appendix and the original statistics come from China Statistical Yearbook (1996-2012) and the statistics consist only 31 provinces of China (exclude Hongkong, Macao and Taiwan). Blue circles are original statistics series, green stars are first fitting values and

red triangles are secondary fitting ones. Secondary fitting is based on the results of first fitting results with the same GM(1,1) model.

### 4.4 Data Analysis and Interpretation

We calculate the residual series and find that the second processing results are better than first fitting in most provinces. The residual series represent the relative errors when fitting which can to some degree reflect the accuracy of results. The little the values are, the more credible the forecasting differential equations are. To be clear, the residual series results are based on the secondary fitting curves.

PROVINCES	Beijing	Hebei	Jilin	Heilongjiang	Anhui	Guizhou
FIRST	4.87%	5.16%	9.93%	6.76%	5.79%	9.35%
SECOND	1.18%	1.46%	5.25%	1.99%	2.56%	2.04%
PROVINCES	Jiangxi	Hunan	Guangdong	Hainan	Sichuan	Xizang
FIRST	13.30%	4.82%	10.72%	9.15%	5.34%	10.18%
SECOND	2.50%	1.73%	0.90%	5.86%	0.84%	5.66%

Table 1: Residual Series List 1

The reasons of two different results are the real circumstances of certain provinces. For example, observing pictures directly we can find that data of certain provinces are in accordance with GM(1,1) model and has the same trend both in urban area and reginal area, such as Beijing, Hunan, Guangdong, Xizang, but some others are not. The probable reason is that in these provinces, the urbanization is increasing rapidly and water assumption from urban area occupy



Figure 1: Beijing







Figure 3: Jilin



Figure 4: Heilongjiang









Figure 7: Jiangxi











Figure 10: Hainan



Figure 12: Xizang

a huge part of total amount. However, provinces like Jilin, Anhui, Guizhou, Jiangxi, Hunan, Sichuan, most of which consist of major farmland of China show an opposite trend of two results. Data from Hebei and Heilongjiang show a turbulent regulation, possibly because of their vast area and population.

A few provinces, i.e. Neimeng, Jiangsu, Qinghai, illustrate that merely considering urban water needs will be more fitful to GM(1,1) model. Their residual series are showed in following table and pictures.

Table 2: Residual Series List 2									
PROVINCES	Neimeng	Jiangsu	Qinghai						
FIRST SECOND	4.17% 6.20%	3.51% 5.62%	4.35% 13.71%						

Neimeng and Qinghai provinces are vast in territory and major population concentrates in urban area. On the other hand, natural environment is worse in these area, possibly causing turbulent trend or statistic errors of data. Jiangsu may be just an exception.











Figure 15: Qinghai

Besides, we as well find that both first fitting and secondary fitting curves (i.e. green stars data and red triangle data) have a similar trend but the secondary fitting values have higher accuracy by checking residual series results. We do not give the whole results here and choose secondary fitting values to do the next model.

# 5 Nonlinear Programming

If the objective function or constraints include nonlinear function, this kind of programming problem is called nonlinear programming problem. In general, it is harder to solve nonlinear programming problems than linear ones. Unlike linear programming problems which have the simplex method as a universal method, each method for nonlinear programming has its own specific conditions and ranges for problems.

For a practical issue, we should consider following points before boiling problems down to nonlinear programming ones

• Determine alternative strategies

First, get relevant information and data about issues and be familiar with the background. Then choose the alternative strategies and express them as sets;

• Provide objective

After analyzing data and background of the problem, provide objective of minimizing or maximizing. Make mathematical model to represent objective;

• Make sure the standards of evaluation to the objective

We should have standards to evaluate the advantages and disadvantages of the objective made in the second step. And express these standards as certain quantity forms;

Find constrains

For most problems, we have to find minimum or maximum under certain conditions and constrains. Find all of these constrains and express them as inequalities or equations of variables.

Difference between linear and nonlinear programming

- The optimal solution of linear programming problems merely exits on the boundary of the feasible region (especially on the vertex of the feasible region);
- For nonlinear problems, the optimal solution can exit on any points within the feasible region.

### 5.1 Original Model

Our model is developed from the non-linear programming principle. We focus our model on China. We consider the problem in 31 provinces of China and we use provincial capitals to represent the province as they are typically in need of fresh water rather than other cities in a province in most situations.

Firstly, draw a map showing the provincial capitals with their coordinates; Secondly, assign weights for the cities according to a Topographic map of China. There are eight essential principles for assigning the weights (denote vertical weight by and horizontal weight by and the weight of a city by P)

- $P_h = 0;$
- Every time when the height change (here, "change" means to get the integral of the height) reaches 100 meters, we have  $P_h = P_h + 1$ ;
- If the straight line between two cities cut through a river, we have  $P_h = P_h + 2$ ;
- We say that P<sub>h</sub> = ∞ if the terrain passed by the straight line between that two cities is quite complex especially a mountain area;
- If a city is on a plateauwe have  $P_h = \infty$ ;
- If a third city is exactly on the line between two cities (city *i* and city *j*), we have P<sub>h</sub>(*i*, *j*) = ∞;
- Set the coordinates of city *i* and *j* to be  $(x_i, y_i)$  and  $(x_j, y_j)$ , then we have  $P_l = \sqrt{(x_i x_j)^2 + (y_i y_j)^2}$ ;
- $P = k_1 P_l + k_2 P_h$ , where  $k_1 + k_2 = 1$ ; in our experiment, we take  $k_1 = 0.05, k_2 = 0.95$ .



Figure 16: *Pl* of 31 Provinces

Seijing	111	0	0	111	10	10	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	18	111	111	111	111
Tianjin	0	111	0	111	111	111	111	111	111	111	111	111	111	111	0	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	11
lebei	0	0	111	10	10	111	111	111	111	111	111	0	111	6	0	0	111	111	111	111	111	111	111	111	111	111	15	111	111	111	111
Shanzi	111	111	10	111	5	111	111	111	111	111	111	111	111	111	10	10	111	111	111	111	111	111	111	111	111	111	111	111	111	19	11
Neimeng	10	111	10	5	111	10	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	12	111
Lisoning	10	111	111	111	10	111	2	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111
Jilin	111	111	111	111	111	2	111	2	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111
Heilong,	111	111	111	111	111	111	2	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111
Shangha:	111	111	111	111	111	111	111	111	111	0	0	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111
Jiangsu	111	111	111	111	111	111	111	111	0	111	0	0	111	111	4	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111
Zhejiang	111	111	111	111	111	111	111	111	0	0	111	4	111	10	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111
Anhui	111	111	0	111	111	111	111	111	111	0	4	111	111	0	4	0	10	111	111	111	111	111	111	111	111	111	111	111	111	111	111
Fujian	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111
Jiangzi	111	111	6	111	111	111	111	111	111	111	10	0	111	111	111	111	0	0	111	111	111	111	111	111	111	111	111	111	111	111	111
Shandong	111	0	0	10	111	111	111	111	111	4	111	4	111	111	111	0	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111
Henan	111	111	0	10	111	111	111	111	111	111	111	0	111	111	0	111	0	111	111	111	111	111	111	111	111	111	15	111	111	111	111
Rubei	111	111	111	111	111	111	111	111	111	111	111	10	111	0	111	0	111	0	111	111	111	111	111	111	111	111	111	111	111	111	111
Hunan	111	111	111	111	111	111	111	111	111	111	111	111	111	0	111	111	0	111	111	111	111	111	111	111	111	111	111	111	111	111	111
Guangdos	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	S	111	111	111	111	111	111	111	111	111	111	111
Guangzi	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	S	111	111	111	111	111	111	111	111	111	111	111	111
Hainan	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111
Chongqis	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111
Sichuan	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111
Guizhou	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	30	111	111	111	111	111	111
Yunnan	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	30	111	111	111	111	111	111	111
Tibet	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111
Shannzi	18	111	18	111	111	111	111	111	111	111	111	111	111	111	111	15	111	111	111	111	111	111	111	111	111	111	111	111	111	13	111
Gansu	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	0	10	111
Qinghai	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	0	111	30	111
Ningxia	111	111	111	19	12	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	13	10	30	111	111
Xinjian;	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111	111

Figure 17: *Ph* between the 31 Provincial Capitals



Figure 18: China Graphical Map



Figure 19: *P* of 31 Provinces

### 5.2 Shortest Path Problem Model

#### 5.2.1 The background

Shortest path problem is to find the shortest distance on a certain net between two points and the distance here is a joint name of arc (side) weights, it can be time or fees etc.

#### 5.2.2 Dijkstra algorithm

Generally, problem of shortest path can be described as following: We are given a weighted directed graph D = (V, E, W) (also known as the "net"). As for each arc  $(v_i, v_j)$ , correspondingly we have weight  $w_i j$ .  $v_s, v_t$  are two fixed points in D, assuming that P is a path from  $v_s$  to  $v_t$ , now define the weight of path P as the sum of all the arcs on the path, we record this as  $\omega(P)$ . Shortest path problem is to find a path holding the minimum weight among the paths between  $v_s$  and  $v_t$ , which means to find a path  $P_0$  from  $v_s$  to  $v_t$  so that we have

$$\omega(P_0) = \min_{P_0} \omega(P_0) \tag{9}$$

And the formula (9) fits the demand that  $P_0$  is the minimum path from  $v_s$  to  $v_t$ .

When facing ordinary net problems, we can list all the possible paths and find the shortest one by the method of comparison. However, when it comes to some complex problems, the method above may not be feasible and then we need to find a new calculation method. Up till now the best way to find the shortest path in an all-positive-arc directed weighted network is the *Dijkstra* method.

Essential principle of *Dijkstra* is as follows: if  $(v_1, v_2, ..., v_n)$  is the shortest path from  $v_s$  to  $v_t$  then  $(v_1, v_2, ..., v_{n-1})$  is the shortest path from  $v_1$  to  $v_{n-1}$ .

Assuming that in the network of  $D = (V, E, W)(v_1, v_2, ..., v_n)$  weight of arc  $(v_i, v_j)w_{ij}$  represents the direct distance from  $v_i$  to  $v_j$  when there is no direct arc from  $v_i$  to  $v_jw_{ij} = +\infty$  we use  $d(v_j)$  to represent the weight of the path passing those chosen points from only from  $v_1$  to  $v_j$ . The specific steps of *Dijkstra* method finding the shortest path from  $v_1$  towards other vertexes are as follows

- $d(v_1) = 0, d(v_j)\omega_{1j}$  (j = 2, 3, ..., n), S = 1, R = 2, 3, ..., n, mark number from  $v_1$ , each mark consists of two parts, the former one shows its origin and the latter shows the shortest distance between the point and  $v_1$ .
- Search in *R* for vertex *v*so that

$$d(v_k) = \min d(v_j) \tag{10}$$

Make  $S = S \cup kR = R/k$ , and mark number for  $v_k$ . if  $R = \emptyset$  end her; otherwise, come to next step.

• Revise  $d(v_j)$  so as to get

$$d(v_i) = \min\{d(v_i), d(v_k) + \omega_{ki}\}$$

$$(11)$$

Notice that remember the front point of  $v_j$ , return to the second step.

Via the principle of shortest path method, we have a graph showing the minimum distances between each two provinces. Our objective function is  $g(x) = \frac{1}{2} \sum_{i,j} |f_{ij}| d_{ij}$ .



Figure 20: Final Result Showing Our Water Transfer Scheme

Our final water strategy has been showed in the table, and transferring links have been labeled on China regional map.



Figure 21: Our Water Transfer Scheme Showing on Map

Table 3: Water Strategy											
Province	Resource	Water Demand	Inflow Transmission								
Beijing	15.98	31.3	15.32								
Tianjin	4.42	15.70	11.27								
Hebei	13.38	50.30	36.91								
Shanxi	86.35	86.35	0								
Inner Mongolia	284.47	188.00	0								
Liaoning	204.97	79.2	0								
Jilin	242.05	83.60	0								
Heilongjiang	379.88	80.2	0								
Shanghai	3.95	142.90	138.94								
Jiangsu	188.17	311.80	123.62								
Zhejiang	650.31	133.00	-138.94								
Anhui	435.54	281.10	-123.62								
Fujian	677.65	181.10	0								
Jiangxi	886.85	143.10	0.01								
Shandong	192.86	85.00	-62.84								
Henan	202.38	172.60	-0.66								
Guangdong	1243.78	290.10	0								
Guangxi	1155.45	218.80	0								
Hainan	450.22	13.70	0								
Chongqing	494.74	155.50	0								
Sichuan	2112.23	138.6	0								
Guizhou	575.97	76.90	0								
Yunnan	1384.88	111.80	0								
Tibet	4370.98	6.60	0								
Shannxi	548.94	34.30	0								
Gansu	147.92	30.60	-69.38								
Qinghai	709.93	8.20	0								
Ningxia	-56.28	13.10	69.38								
Xinjiang	401.00	59.20	0								

# 6 Optimization Model for Nonlinear Programming

### 6.1 AHP Background

AHP (Analytic Hierarchy Process) is a basic method resolving some complex or obscure problems. AHP fits well with those questions that are hard to make it quantitatively.

Roughlyit can be divided into five steps

- View the question as a hierarchy including the decision objective, the alternatives of reaching it, and the criteria for evaluating the alternatives;
- Set up priorities among the elements of the hierarchy by creating a series of judgments based on pairwise comparisons of the elements. For instance, when comparing potential real-estate purchases, the investors may say they prefer location over price and price over timing;
- Synthesize these judgments to control a set of overall priorities for the hierarchy. This may combine the investors' judgments about location, price and timing for properties A, B, C, and D into overall priorities for each property;
- Check the consistency of the judgments;
- (v) Get a final decision based on the results of this process.

### 6.2 Multi-objective Linear Weighting Function

The function of multi-objective linear weighting function method is

$$R = \sum_{i=1}^{2} \left(\sum_{j=1}^{n} x_i \frac{r_j}{z_j}\right) w_i$$
(12)

R is the total score.

 $x_i$  is the actual value of a certain single index;

- $z_i$  is the standard value of a certain index;
- $r_j$  is the weight of a certain index in the *j*th level;
- $w_i$  is the weight of both ecological and social economy.

### 6.3 Optimal Model and Data Interpretation

In the original nonlinear programming model, one basic assumption is that most of water resource can be explored and utilized by local people. Considering more factors such as water quality, population and economic influence. Thus we adopt *Multi-objective linear weighted function method* to take these factors account by influencing available water. The modified objective function is

$$\max \sum_{i=1}^{31} \left[ (a_i + \sum_{j=1}^{31} f_{ij}) (w_1 s_{1i} + w_2 s_{2i} + w_3 s_{3i} + w_4 s_{4i}) \right]$$
(13)

in which the evaluation function is

$$R = \sum_{i} (w_1 s_{1i} + w_2 s_{2i} + w_3 s_{3i} + w_4 s_{4i})$$
(14)

 $w_1, w_2, w_3, w_4$  are the weight of water quality, water supply, population and economy, respectively.

Considering the huge amount of data results of this model and limited time for writing, we state the main optimal results from this model.

- In North China area, most of provinces receive much water supply from south area where precipitation and runoff volume are abundant. For example, Tianjin receive  $128.85 * 10^8 m^3$  more water. In addition, the results should that some regions like Tianjin, Shanghai, Jiangsu, Guangdong increase their disposable water. These regions are mostly developed ones who have prominent GDP and huge amount of population. Increasing water supply to these area will improve the development of industry and agriculture.
- In terms of origins of water, southeast provinces like Jiangxi, Hubei, Hunan transfer more water (74.3, 34.0, 74.2 billion  $m^3$  respectively). These provinces have abundant water resource and flat terrain. Thus, the cost of transmission facilities will be relatively low.
- A few provinces (e.g. Inner Mongolia, Guangxi) have solve their own water shortage by increasing linking with other areas.





Table 4: Water Strategy										
Province	Resource	Water Demand	Inflow Transmission							
Beijing	15.98	31.30	31.30							
Tianjin	4.42	15.70	133.32							
Hebei	13.38	50.30	50.30							
Shanxi	86.36	29.50	29.50							
Inner Mongolia	284.47	188.00	188.00							
Liaoning	204.97	79.20	79.20							
Jilin	242.05	83.60	83.60							
Heilongjiang	379.88	80.20	80.20							
Shanghai	3.96	142.90	648.41							
Jiangsu	188.17	311.80	123.62							
Zhejiang	650.32	133.00	133.00							
Anhui	435.55	281.10	281.10							
Fujian	677.66	181.10	677.66							
Jiangxi	886.86	143.10	143.10							
Shandong	192.87	85.00	1013.06							
Henan	202.38	172.60	172.60							
Guangdong	1243.78	290.10	2180.44							
Guangxi	1155.45	218.80	218.80							
Hainan	450.22	13.70	450.22							
Chongqing	494.74	155.50	494.74							
Sichuan	2112.23	138.60	2112.23							
Guizhou	575.98	76.90	575.98							
Yunnan	1384.88	111.80	1384.88							
Tibet	4370.99	6.60	4370.99							
Shannxi	548.95	34.30	34.30							
Gansu	147.93	30.60	30.60							
Qinghai	709.93	8.20	8.20							
Ningxia	-56.29	13.10	1134.67							
Xinjiang	401.01	59.20	401.01							

# 7 Simulation Model

The water strategy we get in the nonlinear programming is a steady-state one based on the prediction results in 2025. We do not give a precise model to describe the whole dispatching strategy between 2013 and 2025. Thus, we apply WEAP (Water Evaluation And Planning System) to build model for simulation in order to observe the dynamic process of dispatching water resource.

WEAP is a software designed for users to model the water supply construction and define relationship of dispatching. Based on the GIS graphical interface, users can rapidly make network model of water sources and demand sites, and then simulate to observe and analyze the results of model. Considering the complexity and accuracy of national water management model, we decide to build a small regional model of North China.

Our model consists of five major provinces: Beijing, Tianjin, Hebei, Shandong and Hunan because of our water dispatching strategy involving these five areas in North China area. North China area is the most water-deficient area of China and the government has been implementing a huge hydraulic engineering called *South-to-North Water Diversion Project* to solve the uneven graphical distribution of water resources. It is also noteworthy that our forecasting water demands of five provinces which cannot be supply from North China is approximate to the amount of water supply of the *South-to-North Water Diversion Project*. To base our model on this special area, we can check our water strategy for a dynamic process.

Water demand of the five provinces in 2013 and 2025 have been showed in the pictures relevant with area of red circle. Results of dynamic water transmission and outflow of every provinces have as well be presented as pictures.



Figure 23: Water Demand

The water demand trend is consistent with results from grey prediction. The



simulation results has been shown in the picture.

Figure 24: Water Demand Per Year in Simulation Model



Figure 25: Water Transmission Links Flow

From the results, we find that transmission from Shandong to Tianjian presents an increasing trend which means that during 13 years, the water dispatching strategy should adjust amount of transferring instead of being constant. In further, this result tells us that our water strategy getting from programming based on forecasting values has been optimized.



Figure 26: Dynamic Water Strategy

# 8 Defects of Our Models

- In the nonlinear programming model, we ignored the water used on agriculture for its difficulty to forecast;
- The objective function has a positive correlation with water transferring cost, but we ignored the real cost, which is much too idealistic;
- Strictly speaking, we choose provinces as elements instead of drainage which may be more fitful for forecasting;
- We ignored factors like price, environment, etc. These factors may be prominent in certain region or in certain time;
- In the nonlinear programming model, we consider only the straight lines between cities, which is not flexible. Plus, we concentrate all amount of water into provincial capitals, which may cause errors to some degree.

# 9 Conclusion

In this article, we build some theocratical models and one simulation model to find the best water dispatch and transfer strategy. Firstly, we use grey prediction to forecast the future water needs. Then based on results and other statistics, we build nonlinear programming model to make optimal strategy. Afterwards, we consider more factors and modify our original objective function. The final results of optimal model illustrate a more rational strategy relating to China's *South-to-North Water Diversion Project* and show a better water managing scheme than previous one.

# References

- [1] Ynajun Dong. 2007. Study on the theory and application of middle route of south-to-north water transfer project supply dispatching. *China Institute of Water Resources and Hydropower doctoral thesis*.
- [2] China's National Bureau of Statistics. China Statistical Yearbook. http://www.stats.gov.cn/tjsj/ndsj/
- [3] Ines Winz, Gary Brierley, Sam Trowsdale. The Use of System Dynamics Simulation in Water Resources Management. Water Resour Manage (2009) 23:1301C1323
- [4] WEAP Features. http://www.weap21.org/index.asp?action=202
- [5] Analytic hierarchy process. http://dict.bing.com.cn/#%E5%8F%B0%E6%B9%BE

# 10 Position Paper for China Government

To whom it may concern:

Based on our model of water resource management, we sincerely recommend you to implement some water strategies to meet water needs in 2025.

- According to our results of prediction, the trend of water needs of different provinces will be different before 2025. For Beijing, Heilongjiang, Guangdong, Hainan, Jiangsu, the water needs will increase and the major part may come from urban area. For Jilin, Anhui, Guizhou, Jiangxi, Hunan, Sichuan, Neimeng, these provinces will need to prepare more water for rural people and urban water demand may decrease.
- During next decade, building or encouraging desalination facilities is necessary for some southeast costal provinces such as Shanghai, Guangdong, Fujian, Hainan. This implementation will provide alternative demands for their own use.
- Keep on South-to-North Water Diversion Project which will solve most of water shortage in North China. In addition, pay attention to real-time demands changes from different provinces and build small-scale transmission to keep balance.
- Improve recovery efficiency of local water resource including both surface and underground water and it will make most of provinces keep their own balance of using water.

Most of these strategies are based on the present conditions and facilities, so you can adopt them as soon as possible. Plus, during making model, what we consider first is to make every area self-sufficient and the cost of other projects has been reduced. China has a huge population and water resource problems involve complex factors. Our model is based on major factors after carefully analyzing statistics. Not only China's present hydraulic project is taken into account, but also researches and experience from other countries are considered through analyzing review papers.

> Best Regards, Team 22862 Feb 4, 2013